## PHYS 451 Quantum Mechanics II (Fall 2018) Quiz #2

Consider a particle of mass m moving in an infinite square well potential,

$$V(x) = \begin{cases} 0, & 0 \le x \le a \\ \infty, & \text{otherwise} \end{cases}.$$

The system is now subjected to a perturbation in the form

$$H' = \begin{cases} \beta, & 0 \le x \le a \\ \gamma, & \text{otherwise} \end{cases},$$

where  $\beta$  and  $\gamma$  are constants. Treat this perturbed system in the framework of the perturbation theory and answer the following questions:

- 1. Is there any restriction on the values of  $\beta$  and  $\gamma$  so that the application of the perturbation theory remains valid? Be specific, i.e. do not just say  $\beta$  must be large or small.
- 2. What is the first-order correction to the energy of the n-th state?
- 3. What is the second-order correction to the energy of the ground state?
- 4. Do the results you obtained in parts 2 and 3 make sense? Why?