PHYS 451 Quantum Mechanics II (Fall 2018) Quiz #4

A particle of mass m is trapped in a 2D infinite square well (0 < x < a, 0 < y < a). Inside the well there is a small sharp bump in the form:

$$V(x,y) = \beta \,\delta(x - a/4) \,\delta(y - a/4),$$

where $\delta(...)$ is the Dirac delta function and β is a small positive constant.

- 1. How small must β be so that the perturbation theory is applicable?
- 2. Consider the first excited state of this system. Find the first-order correction to its energy.